

# Determination of Reference Frame Scale with VLBI

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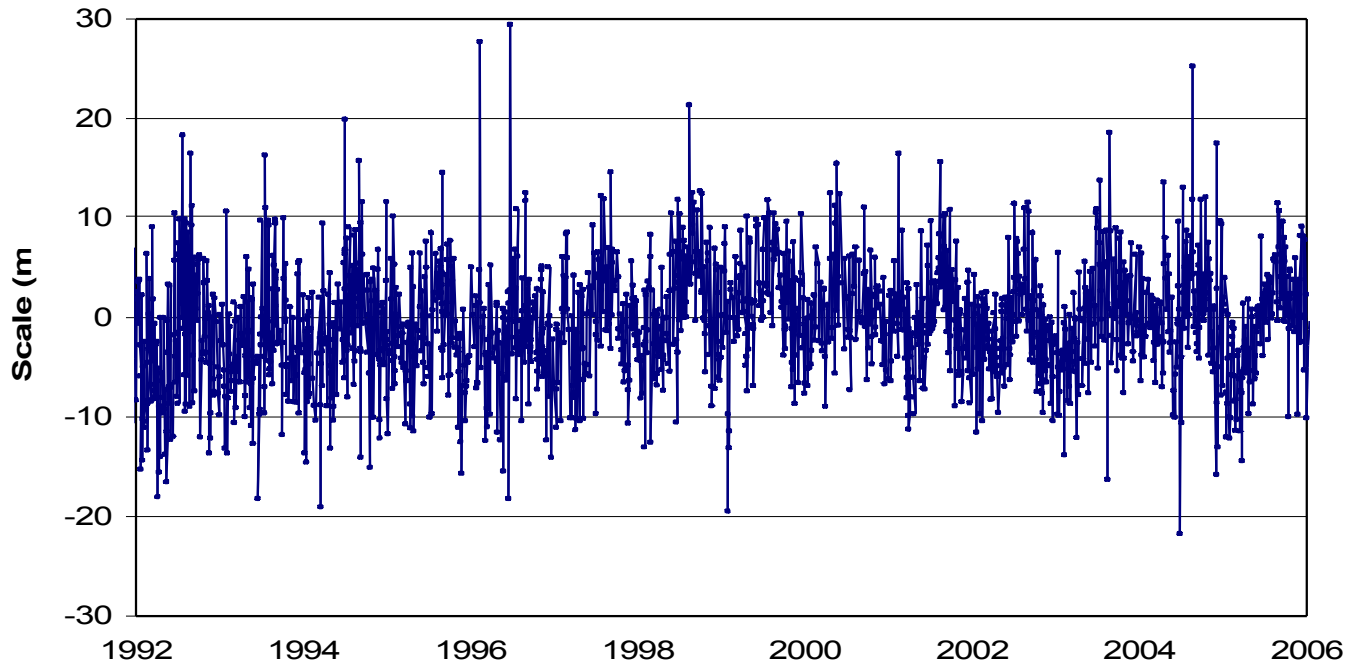
NASA Goddard Space Flight Center

EGU Meeting

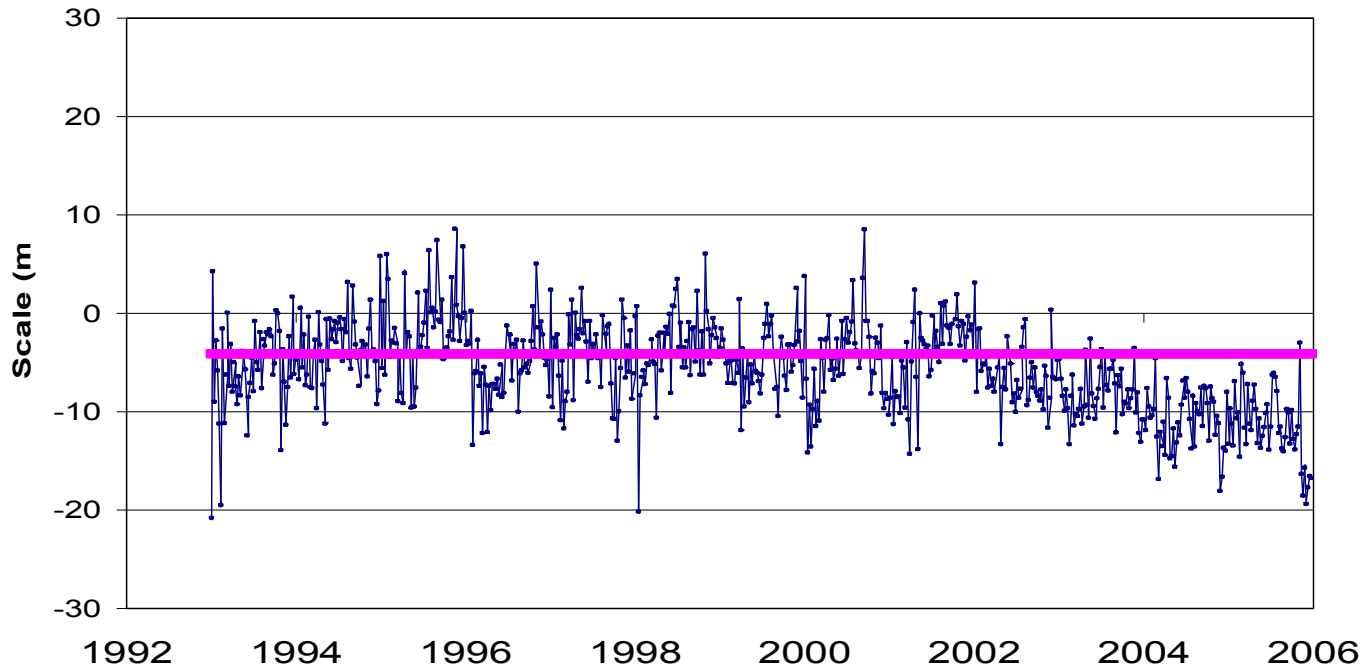
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# Overview

- VLBI – SLR scale difference in ITRF2005
- Systematic effects that contribute to the VLBI scale
- VLBI scale error budget



VLBI daily  
series relative  
to ITRF2005



SLR weekly  
series relative  
to ITRF2005

1993-2002 bias  
= -4.3 mm

=> -0.68 ppb

# Systematic Errors Contributing to VLBI Scale

- Antenna Thermal Deformation
- Pressure Loading and Hydrology Loading
- Atmospheric Delay Modeling
- Radio source structure
- Pole tide

# Antenna Thermal Deformation

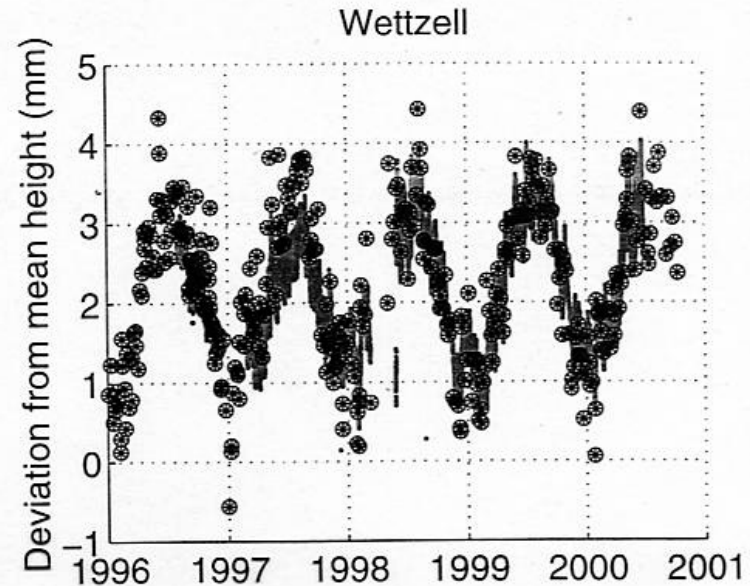
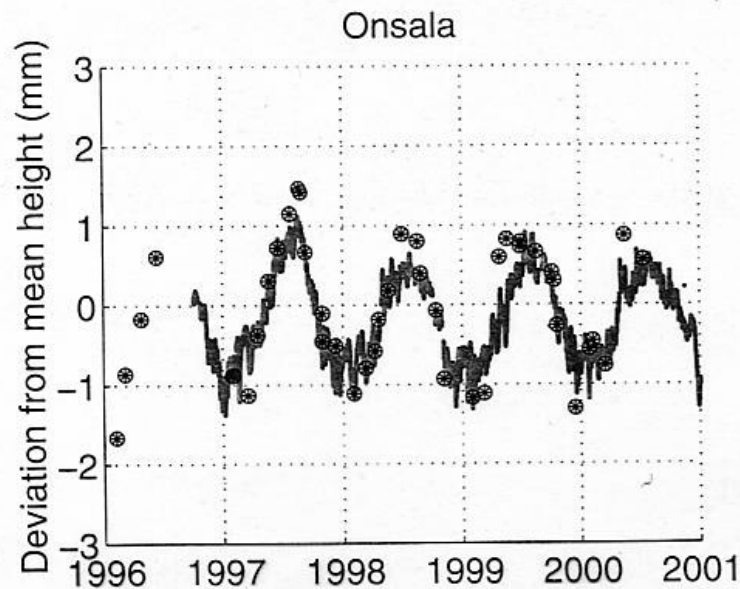
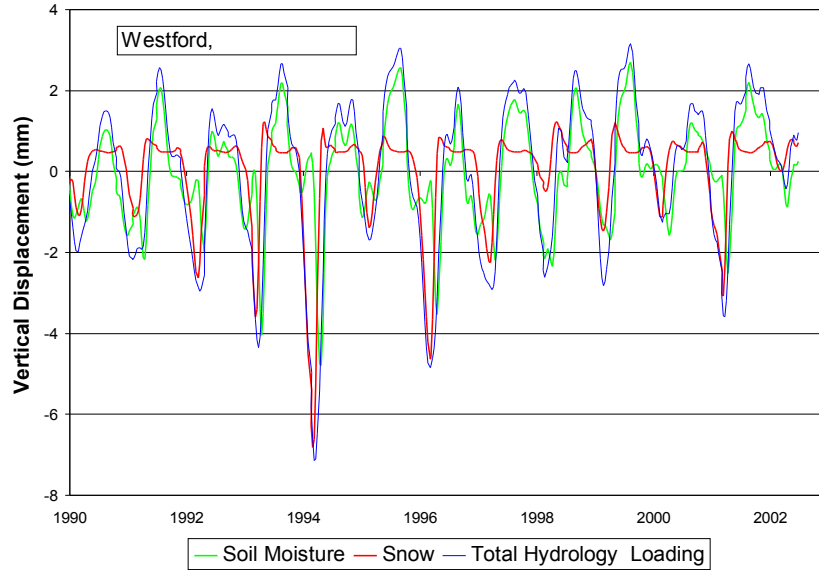


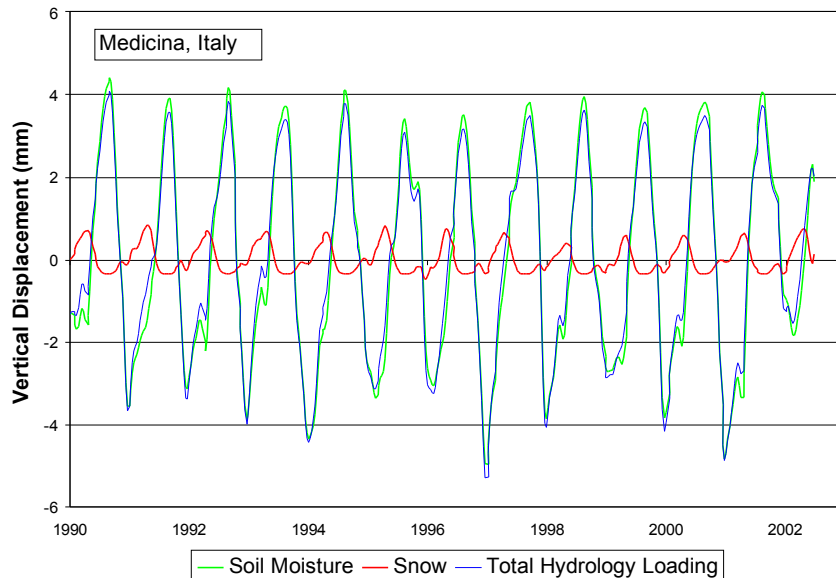
Figure 13: Vertical height changes of the VLBI radio telescopes at Onsala and Wettzell: solid lines - measured by the invar rod measuring systems; stars in circles - modelled with a simple model based on daily mean temperature from the VLBI data base, thermal expansion coefficient, and the telescope dimensions.

Average vertical bias due to not modeling antenna deformation  
 $\Rightarrow 0.04 \text{ mm} \sim 0.016 \text{ ppb}$

# Hydrology Loading



Loading based on  
Milly Shmakin hydrology  
model



- Scale dependence on hydrology+pressure loading

Effect of pressure loading

$$\Rightarrow 0.006 \pm 0.002 \text{ ppb/yr}$$

$$\Rightarrow -0.05 \pm 0.01 \text{ ppb}$$

Effect of hydrology loading

$$\Rightarrow 0.001 \pm 0.002 \text{ ppb/yr}$$

$$\Rightarrow -0.003 \pm 0.001 \text{ ppb}$$

# Seasonal Length Scale Variation from VLBI

Applying loading contributions to site displacement

=> Small reduction in amplitude

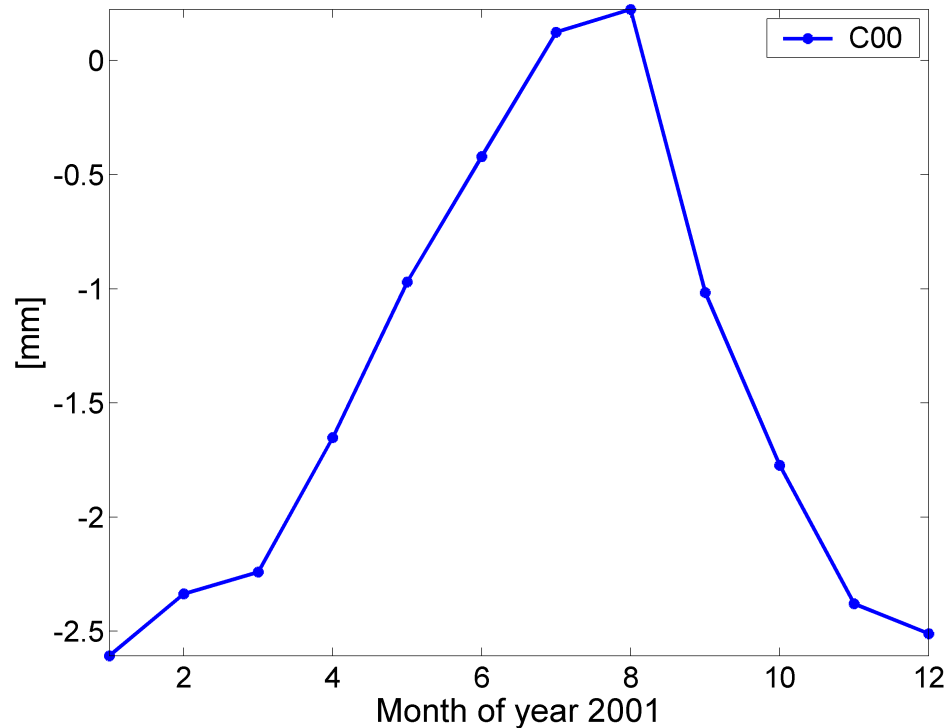
	Annual		Semi annual	
	Amplitude ppb	Phase deg	Amplitude ppb	Phase deg
No Loading	$0.51 \pm 0.03$	$48 \pm 3$	$0.18 \pm 0.03$	$276 \pm 6$
Loading	$0.37 \pm 0.03$	$46 \pm 3$	$0.19 \pm 0.03$	$275 \pm 6$

- Loading contributions include:
- 2) Atmospheric pressure loading
  - 3) Hydrologic loading
  - 4) Non tidal ocean loading



# Atmospheric Delay Modeling Error

Spherical harmonic coefficients of degree 0 (expansion to degree 6)



Scale Difference (VMF – NMF) between frames computed using the VMF or the NMF mapping functions assuming a uniform global coverage of sites.

If only VLBI sites are considered, the peak to peak amplitude is reduced to ~1.25 mm (= 0.2 ppb). [ref. Johannes Boehm]

# Atmospheric Delay Modeling

- Errors in atmospheric modeling at low elevations
- Scale dependence on elevation cutoff

10° - 5° elevation cutoff solutions

=>  $-0.01 \pm 0.005$  ppb/yr

=>  $-0.13 \pm 0.05$  ppb

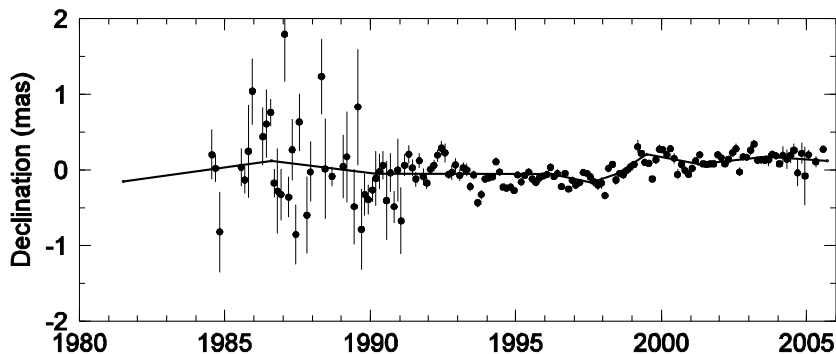
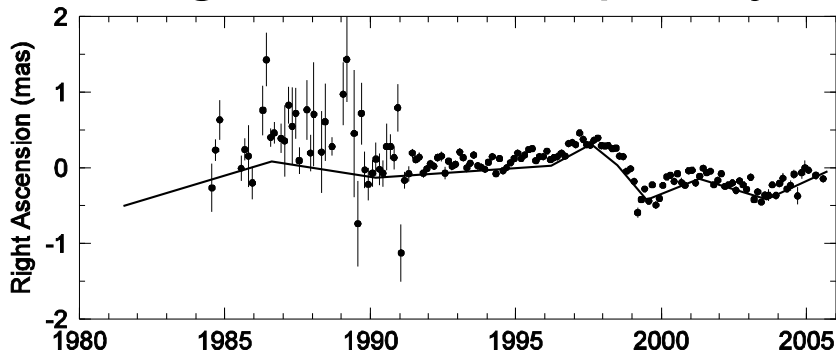
- Mapping function error

VMF – NMF => bias  $\sim -0.1$  ppb

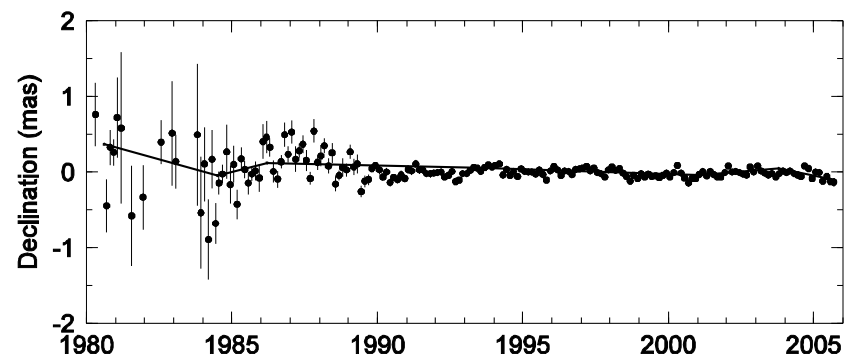
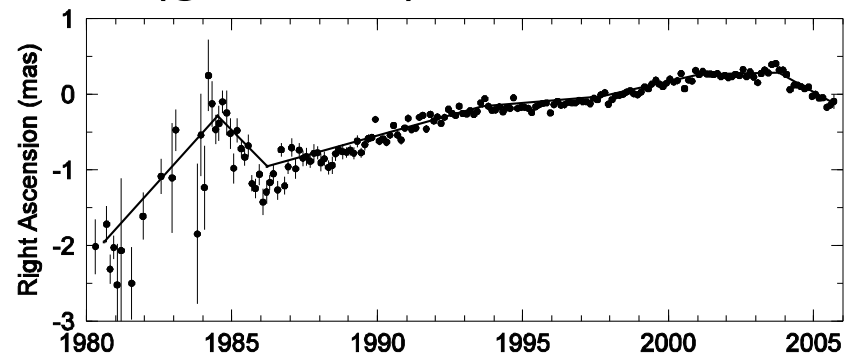
seasonal amplitude  $\sim 0.1$  ppb

# Radio Source Instability

- Radio source position estimates can have large rates or even nonlinear variation
- Identified sources with unstable position time series from among the most frequently observed (geodetic) sources



Radio source 2145+067



Radio source 4C39.25

# Radio Source Instability

- Modeled the position variation of unstable sources either by  
(3) estimating global spline parameters to fit the variation  
or (2) estimating positions for each 24-hour observing session

Effect of radio source instability =>

1) Spline	$-0.02 \pm 0.01$ ppb	$0.004 \pm 0.002$ ppb/yr
2) Local	$-0.02 \pm 0.02$ ppb	$0.008 \pm 0.002$ ppb/yr

# Pole Tide Model

- IERS2003 Convention specifies that a mean pole model referenced to 2000.0 be subtracted from polar motion in computing the deformation effect
- Most (3 out of 4) IVS Analysis Centers did not use this convention in generating their submissions for ITRF2005
- Reference frame scale effect of NOT applying the IERS2003 specification is +0.45 ppb

# Scale Error Budget

Error Source	Annual	Rate ppb/yr	Bias ppb
Thermal Deformation	0.1	---	- 0.02
Loading	0.14	0.01	- 0.05
Atmosphere Modeling	0.1	- 0.01	- 0.13
Radio source instability	---	0.01	- 0.02
Pole Tide	0	0.01	- 0.45* .75
Total	< 0.34	0.02	- 0.54

# Summary

- Most (0.54 ppb) of the scale bias (VLBI-SLR) of 0.68 ppb in ITRF2005 can be explained by inconsistent application pole tide model convention, atmosphere delay model error, and smaller contributions from loading
- VLBI scale has a real annual variation, which is equivalent to modulating the scale by  $\sim 0.5$  ppb, due to annual site variations of various effects (hydrology loading, antenna thermal deformation, etc.) and the predominance of VLBI sites in the Northern hemisphere
- Hydrology loading, pressure loading, antenna thermal deformation, and mapping function error contribute about 0.3 ppb to the annual variation of scale